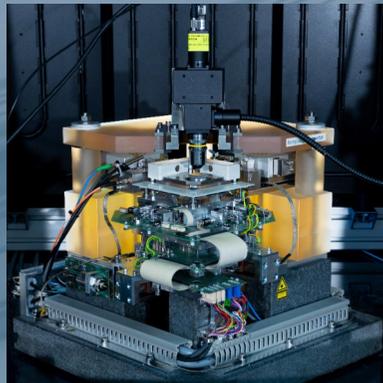
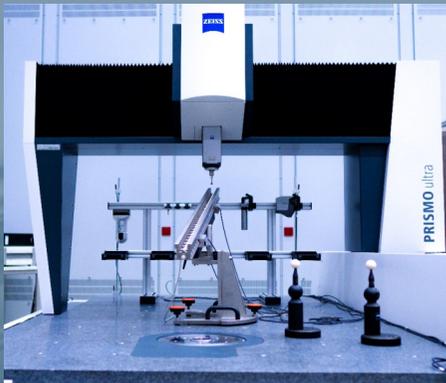


Numerical measurement uncertainty estimation for industrial computed tomography - from basic qualified software for X-ray radiographic simulation tools to numerical measurement uncertainty estimation using a virtual CT system

T. Hausotte

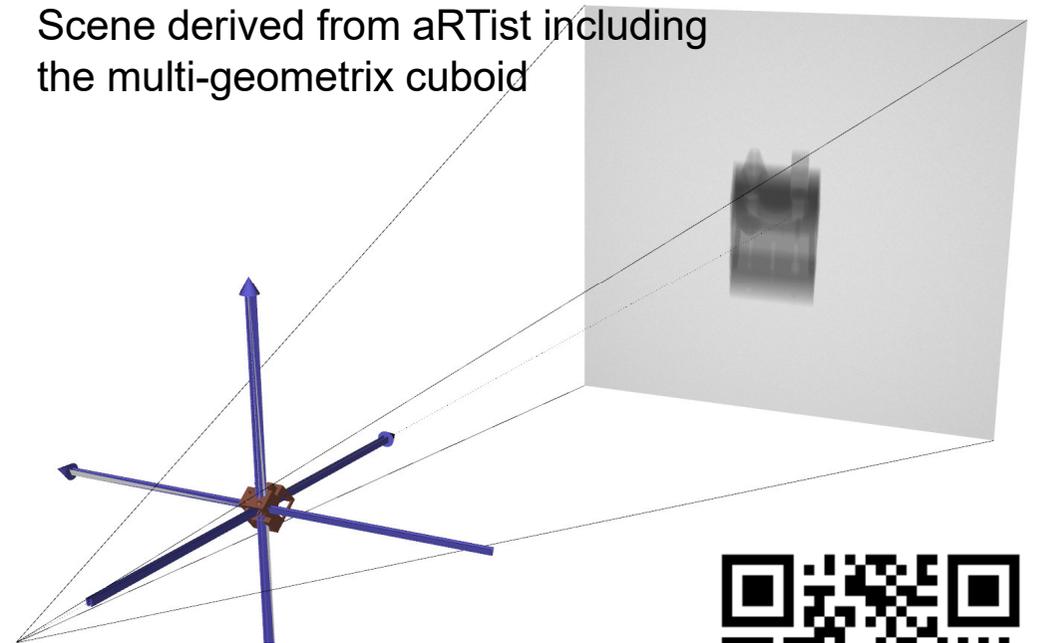
Keynote on **2nd International Workshop on Metrology for Virtual Measuring Instruments (VirtMet2025)**, Online, 03.12.2025



Overview

- 1 Motivation for the CTSimU project series and fundamentals
- 2 CTSimU1: Motivation, objectives, and results
- 3 CTSimU2: Motivation, objectives, and results
- 4 CTSimU3: Motivation, objectives, and approach
- 5 Application of Monte Carlo simulation results for conformity or non-conformity assessment
- 6 Impact of the project series on standardization
- 7 Summary

Scene derived from aRTist including the multi-geometrix cuboid



<https://www.ctsimu.forschung.fau.de/>

Motivation for the CTSimU project series and fundamentals

Increasing use of industrial computed tomography (CT) for coordinate metrology



Demand on accurate and reliable measurements with CT to gain acceptance of CT measurements



Traceability to the metre is the key for accuracy and reliability



Measurement uncertainty determination necessary

How could measurement uncertainty (MU) in industrial CT be determined in principle?



Evaluation of measurement uncertainty with calibrated workpieces



Evaluation of measurement uncertainty using measurement uncertainty budgets



Evaluation of measurement uncertainty through simulation

Standards, guidelines and technical specifications

Relevant standards, guidelines and technical specifications for evaluation of measurement uncertainty



Publications of Joint Committee for Guides in Metrology (JCGM): Guides in Metrology

JCGM 100:2008(E) – in English

Evaluation of measurement data - Guide to the expression of uncertainty in measurement (2008)

JCGM 106:2012

The role of measurement uncertainty in conformity assessment (2012)

JCGM 101:2008

Supplement 1 to the “Guide to the expression of uncertainty in measurement” - Propagation of distributions using a Monte Carlo method (2008)

JCGM GUM-1:2023

Guide to the expression of uncertainty in measurement - Part 1: Introduction (2023)

JCGM 102:2011

Supplement 2 to the “Guide to the expression of uncertainty in measurement” - Extension to any number of output quantities (2011)

JCGM GUM-6:2020

Guide to the expression of uncertainty in measurement - Part 6: Developing and using measurement models (2020)

<https://www.bipm.org/en/committees/jc/jcgm/publications>

Standards, guidelines and technical specifications



Relevant standards, guidelines and technical specifications for evaluation of measurement uncertainty

ISO GPS standards

ISO 14253-2 “Geometrical product specifications (GPS) - Inspection by measurement of workpieces and measuring equipment - Part 2: Guidance for the estimation of uncertainty in GPS measurement, in calibration of measuring equipment and in product verification”

ISO 15530-3 “Geometrical product specifications (GPS) - Coordinate measuring machines (CMM): Technique for determining the uncertainty of measurement - Part 3: Use of calibrated workpieces or measurement standards”

ISO/TS 15530-4 “Geometrical product specifications (GPS). Coordinate measuring machines (CMM). Technique for determining the uncertainty of measurement. Evaluating task-specific measurement uncertainty using simulation”

VDI/VDE standards

VDI/VDE 2617 Part 7 “Accuracy of coordinate measuring machines - Parameters and their checking - Estimation of measurement uncertainty of coordinate measuring machines by means of simulation”

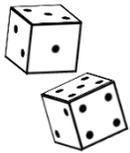
VDI/VDE 2617 Part 11: “Accuracy of coordinate measuring machines - Characteristics and their checking - Determination of the uncertainty of measurement for coordinate measuring machines using uncertainty budgets”

VDI/VDE 2630 Part 2.1 “Computed tomography in dimensional measurement - Determination of the uncertainty of measurement and the test process suitability of coordinate measurement systems with CT sensors”

Only VDI/VDE 2630 Part 2.1 is related to CT!

There are various standards, guidelines and technical specifications for evaluation of the measurement uncertainty, but they

- ➔ cannot be implemented due to the complexity of CT,
- ➔ do not take into account the special features of CT measurements,
- ➔ are time-consuming and resource-intensive (e.g. VDI/VDE 2630 Part 2.1)



Task-specific measurement uncertainty evaluation according to GUM Supplement 1 – Use of the Monte Carlo method

Resource and cost-saving?



- No standardised procedure for
- qualifying simulation software,
 - qualifying digital models and
 - performing a dimensional measurement with uncertainty specification.

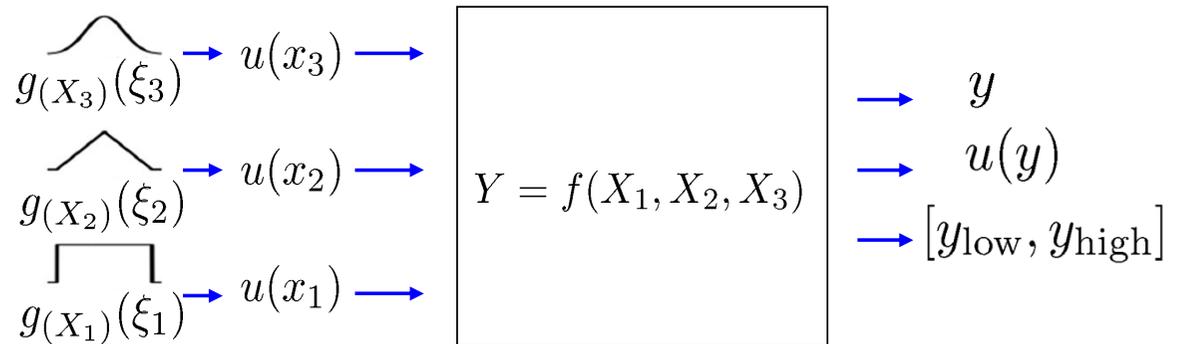
Motivation for the CTSimU project series

Evaluation of measurement uncertainty according to GUM Supplement 1



Measurement uncertainty (GUM standard procedure):

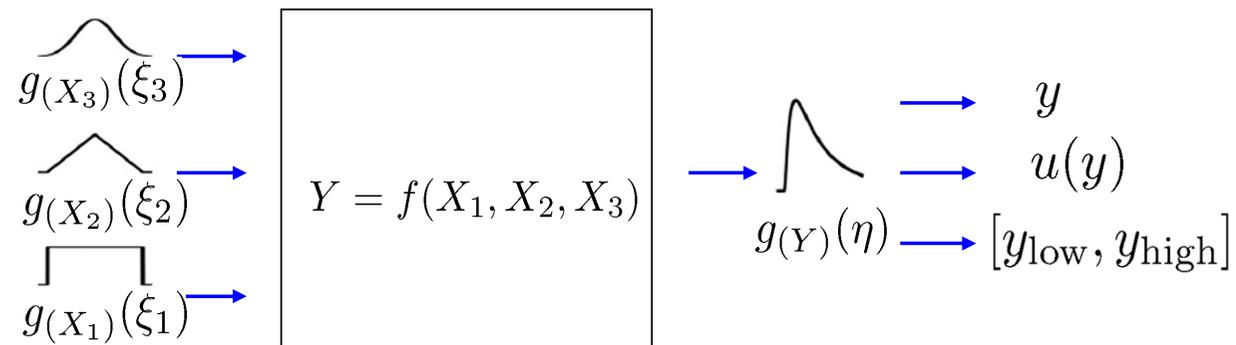
- propagation of the uncertainty values of the influencing factors through an analytical model of the measurement
- central limit theorem and assumption of normal distribution



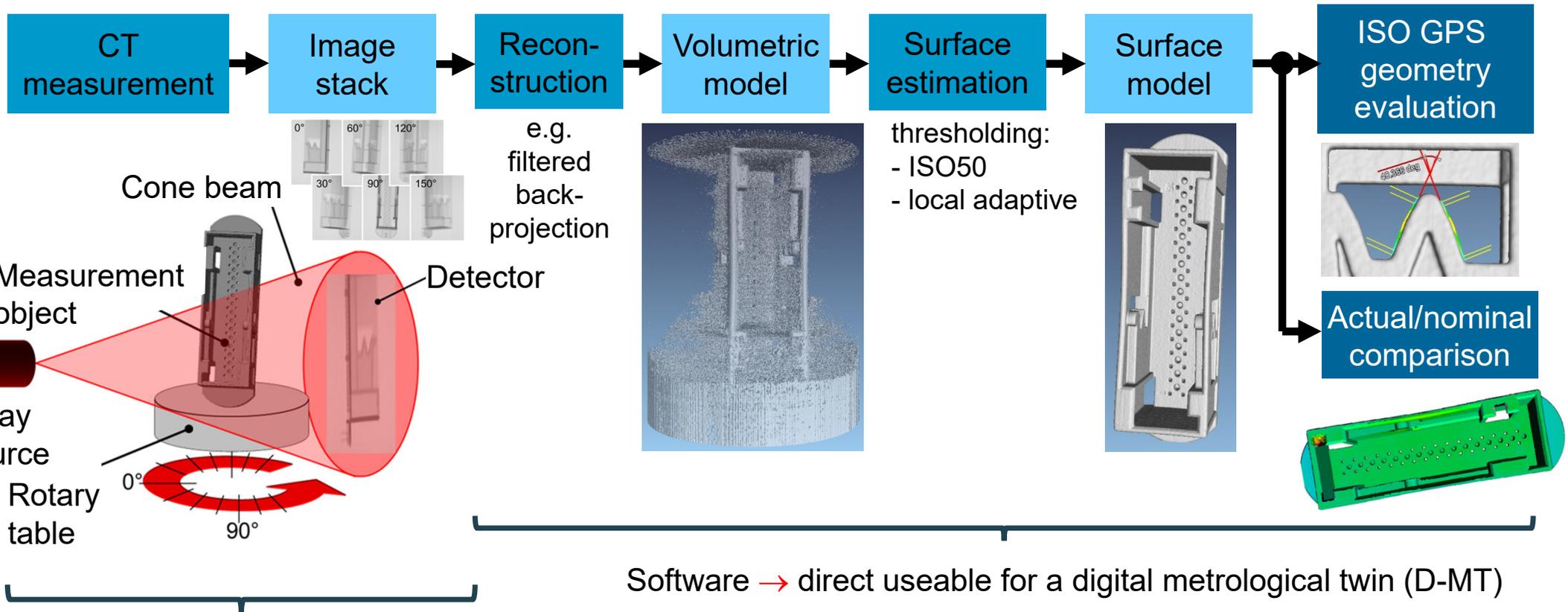
[JCGM 101:2008 Supplement 1]

Measurement uncertainty using the Monte Carlo method:

- propagation of distributions through an analytical or **numerical** model of the measurement
- numerical approximation to the distribution function



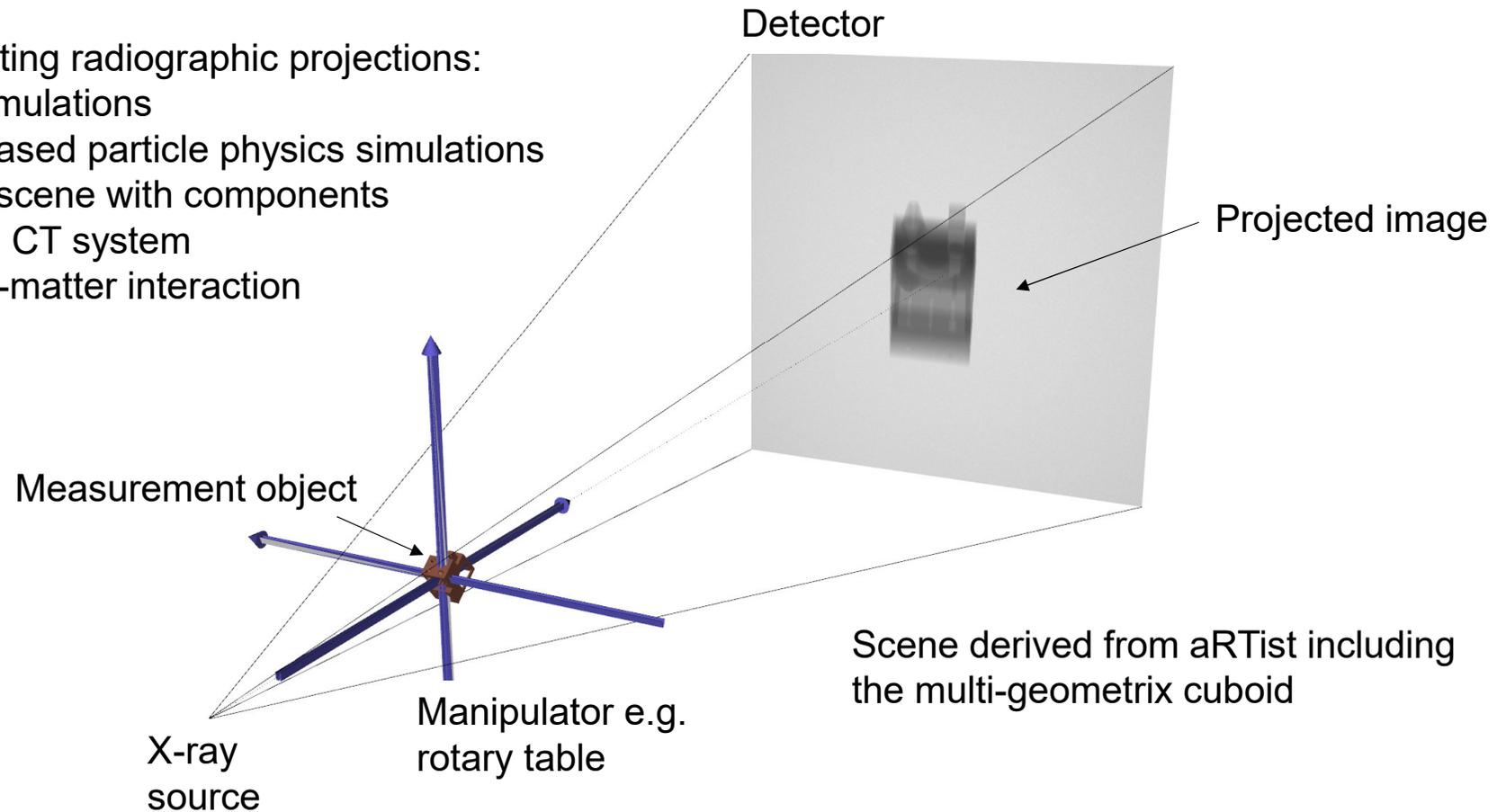
Workflow of dimensional CT measurements



CT system = Hardware → Process must be simulated using a realistic parametrised simulation software

How simulation software works

- Methods for simulating radiographic projections:
 - Ray casting simulations
 - Monte Carlo-based particle physics simulations
- Modelling a virtual scene with components analogous to a real CT system
- Modelling radiation-matter interaction



Structure of the CTSimU project series



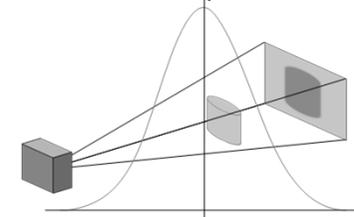
WIPANO – Wissens- und Technologietransfer durch Patente und Normen

<https://www.ptj.de/projektfoerderung/wipano-wissens-und-technologietransfer-durch-patente-und-normen>

CTSimU1



Step 1: Test framework for testing the simulation software with regard to the correct reproduction of relevant physical effects and functionalities



CTSimU2



Step 2: Toolbox for creating a digital model of a CT system and test for verification



CTSimU3

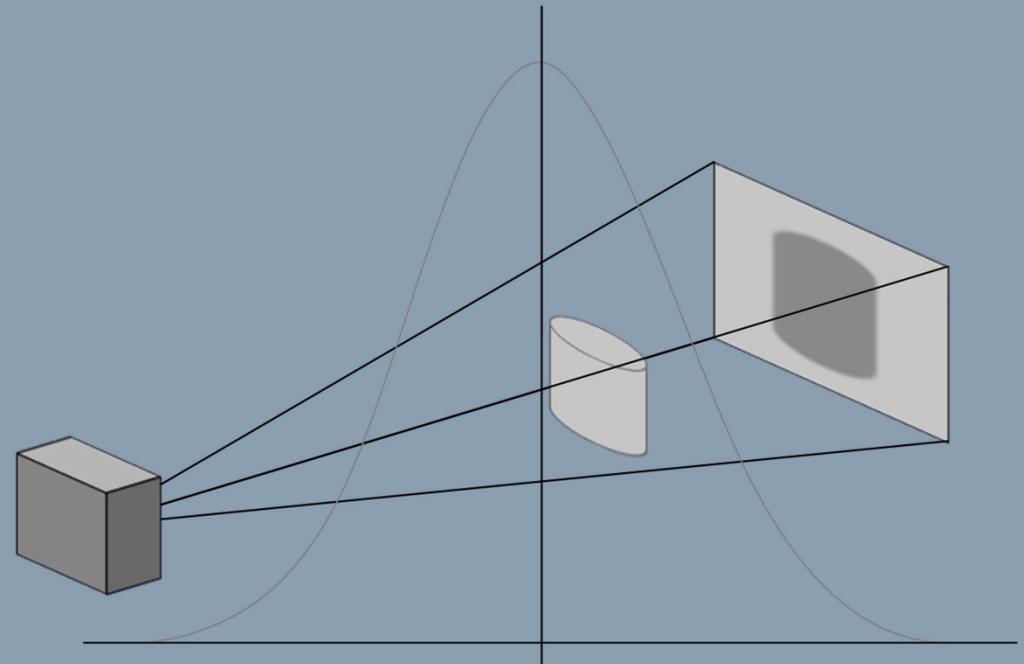


Step 3: Evaluation of the task-specific or measurement-specific measurement uncertainty (MU) by means of simulation using the Monte Carlo method



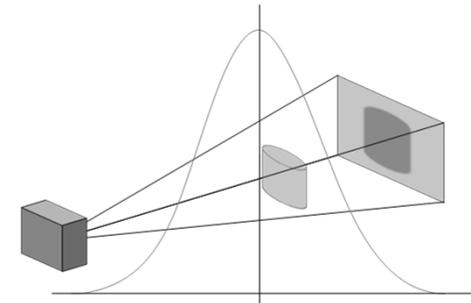
started

CTSimU1



Radiographic simulation for determining measurement uncertainty when measuring geometric features using X-ray computed tomography – basic qualification of simulation software

Consortium: 4 research partners, 5 industrial partners, 1 associated partner



Test framework for testing radiographic simulation software



Basic qualification of the radiographic simulation software

Draft of a standard for VDI/VDE 2630 series 'Computed tomography in dimensional measurement'

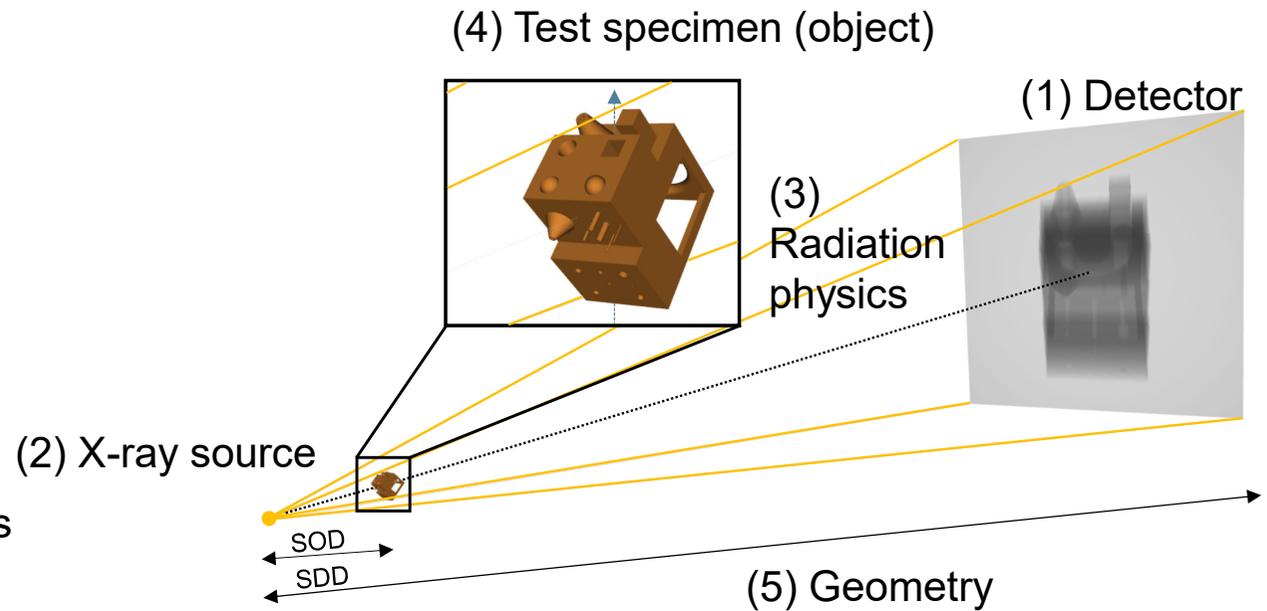


Submission to VDI/VDE-GMA Technical Committee 4.33 'Computed tomography in dimensional measurement' for finalisation

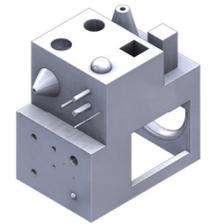
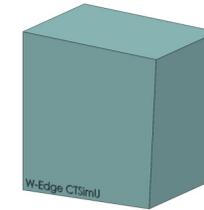
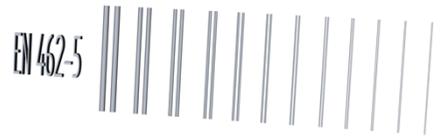
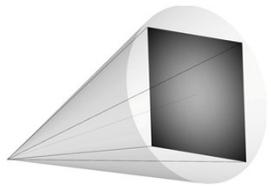
Does simulation software adequately model the relevant physical laws of radiation, radiation-matter interaction and functionalities of CT scans?

Sections regarding:

- (1) Detector of the CT system
- (2) X-ray source of the CT system
- (3) Radiation physics
- (4) Test specimen (object)
- (5) Geometry of the CT system
- (6) Parameters for complete CT scans



Objective: definition of requirements that are essential to conduct a dimensional measurement with a X-ray CT system



Free-beam
(FB)

Conical hole sheet
(HS)

Spherical step wedge
(SW)

Duplex wire
(DW)

Inclined Tungsten edge
(WE)

Multi-geometry cuboid
(3D test)

- Image noise
- Intensity profile

- Position and orientation
 - Object
 - Detector

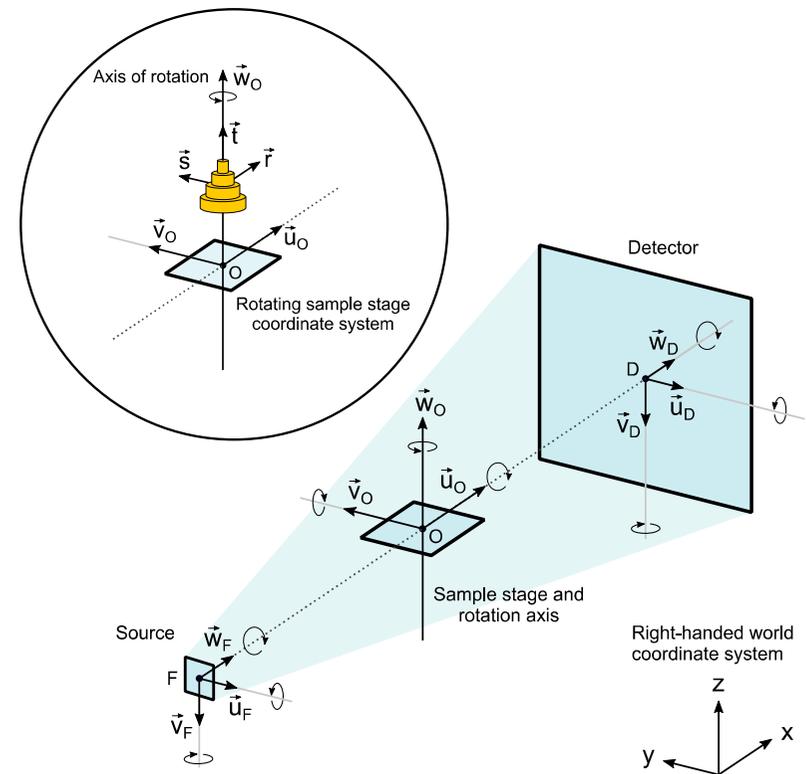
- Material penetration length
- Extinction law, radiation-matter interaction
- Spectral filtering, beam hardening
- Scintillator characteristics
- Adjacent surfaces
- Scattered radiation

- Detector unsharpness

- Partially covered pixels
- Focal spot size

- 3D test involving all steps of the chain

- JSON (Java Script Object Notation) – file interface
- Serves as standardised specification for a complete CT scan:
 - Material
 - CT geometry with variations and deviation
 - X-ray source
 - Detector
 - Scan parameter
 - Test specimen (object)

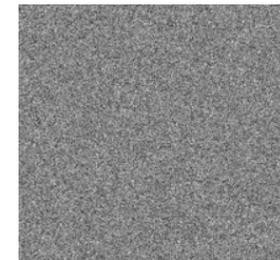
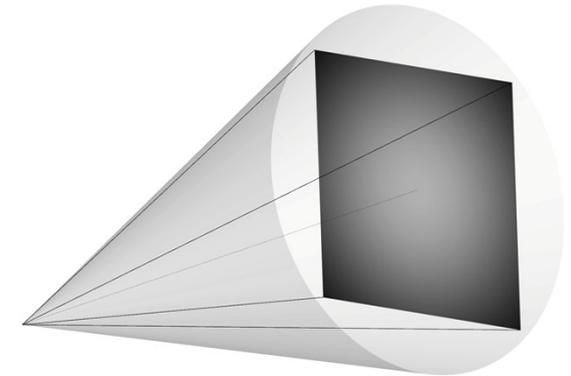
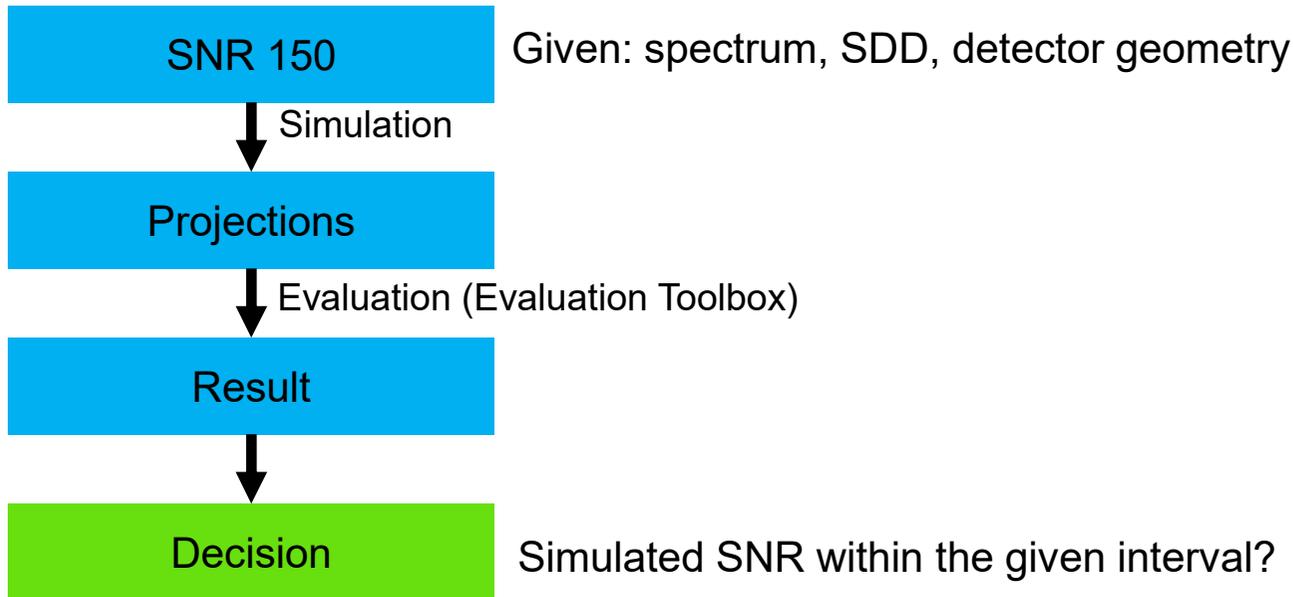


```

"geometry":
{
  "detector":
  {
    "centre": {
      "x": {"value": 400, "unit": "mm", "uncertainty": {"value": 0, "unit": "mm"}, "drift": null},
      "y": {"value": 0, "unit": "mm", "uncertainty": {"value": 0, "unit": "mm"}, "drift": null},
      "z": {"value": 0, "unit": "mm", "uncertainty": {"value": 0, "unit": "mm"}, "drift": null}
    },
    "vector_u": {
      "x": {"value": 0, "drift": null},
      "y": {"value": -1, "drift": null},
      "z": {"value": 0, "drift": null}
    }
  }
}
    
```

CTSimU1

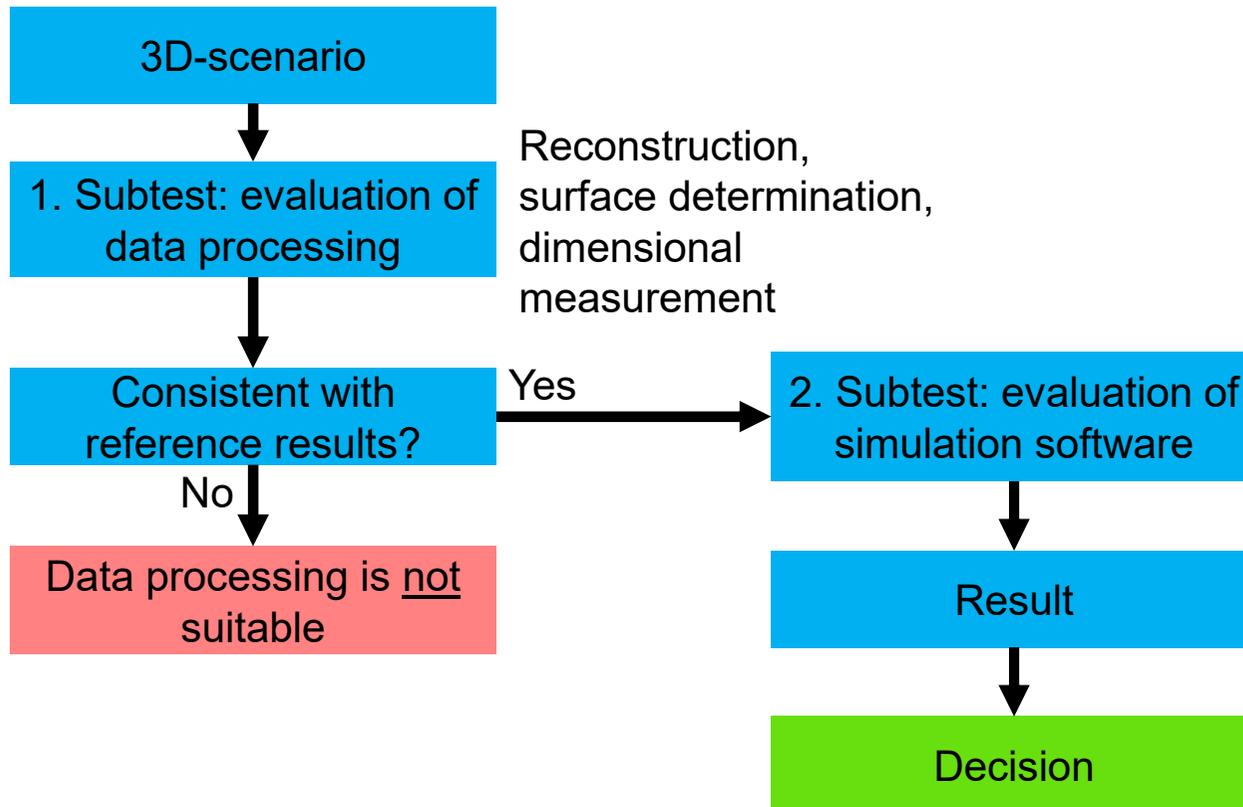
2D test example – Projection noise



SNR 150 at max. intensity

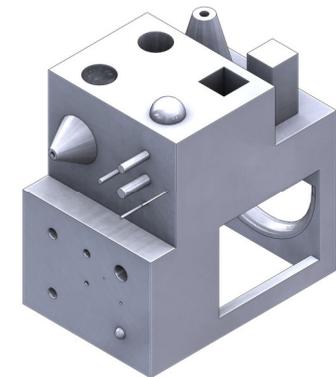
Intervals for acceptable test results: Derived from parameter variations of a 3D scenario

Borges de Oliveira, F.; Reuter, T.; Plotzki, D.; Wohlgemuth, F.; Bartscher, M.; Bellon, C.; Kasperl, S.: Assessment of 2D-based tests for the qualification of simulation software for dXCT 34 (2023) 064005 (12 pp.), DOI 10.1088/1361-6501/acc1f9

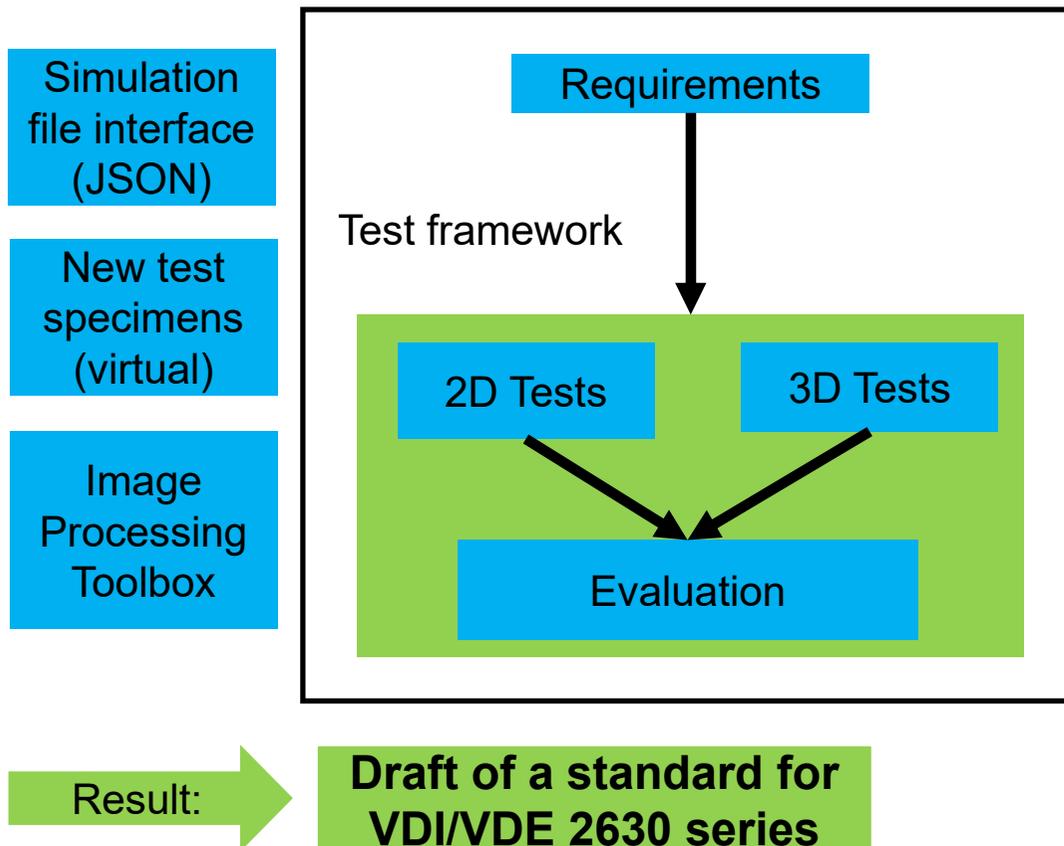


Aim:

- Test of measurement chain
- Test of entire CT Scan
- Test regarding different challenges e.g. noise; detector unsharpness ...



Multi-geometry cuboid



2D Tests:

- 10 scenarios
- 4 different test specimens (virtual)

3D Tests:

- 2 Tests
- 1 test specimen (virtual)

CTSimU evaluation toolbox:

- Reference implementation for 2D tests
- Automated evaluation of 2D tests
- Based on Python

VDI/VDE 2630 Part 2.2:2026-01

Computed tomography in dimensional measurement - Determination of measurement uncertainty by simulation - Basic qualification of software for radiation simulation

CTSimU2



Realistic simulation of real X-ray computed tomography systems with basic simulation software

Consortium: 4 research partners, 7 industrial partners, 1 associated partner



Toolbox with methods for characterising a real CT system and modelling or parameterisation in simulation software



Parameterised digital model of a real CT system

Test to verify whether the digital model accurately reflects the dimensional measurements



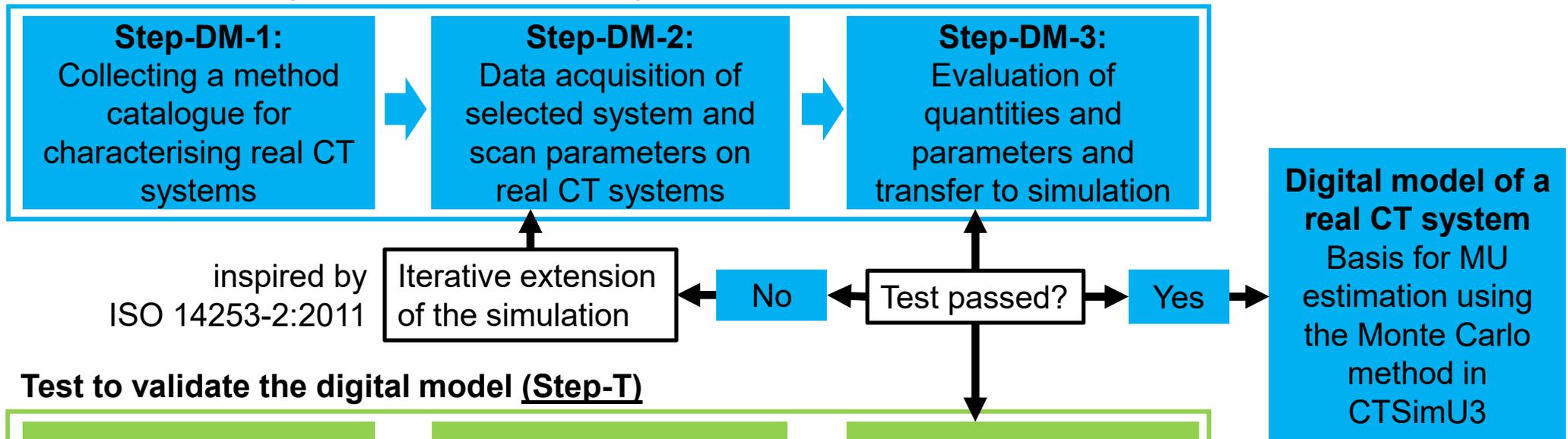
Basic qualification of the digital model of a real CT system

Draft of a standard for VDI/VDE 2630 series 'Computed tomography in dimensional measurement'

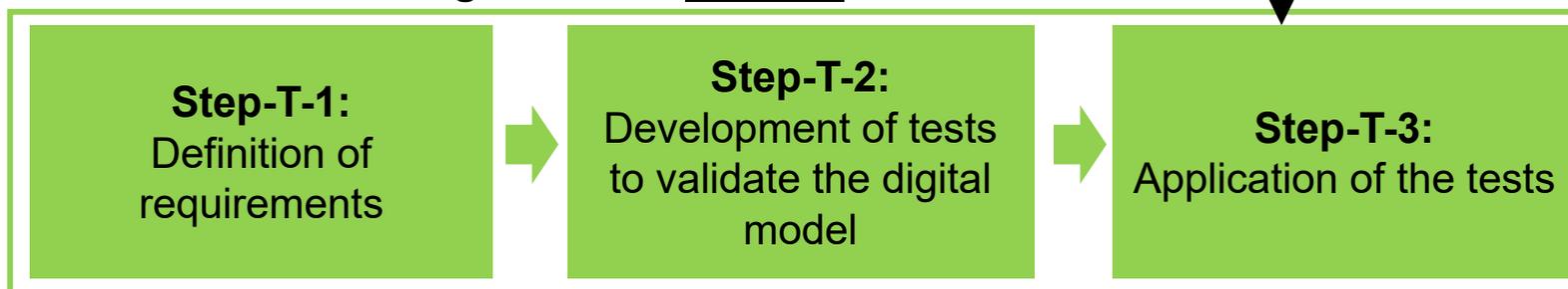


Submission to VDI/VDE-GMA Technical Committee 4.33 'Computed tomography in dimensional measurement' for finalisation

Creation of the digital model of real CT system (Step-DM)



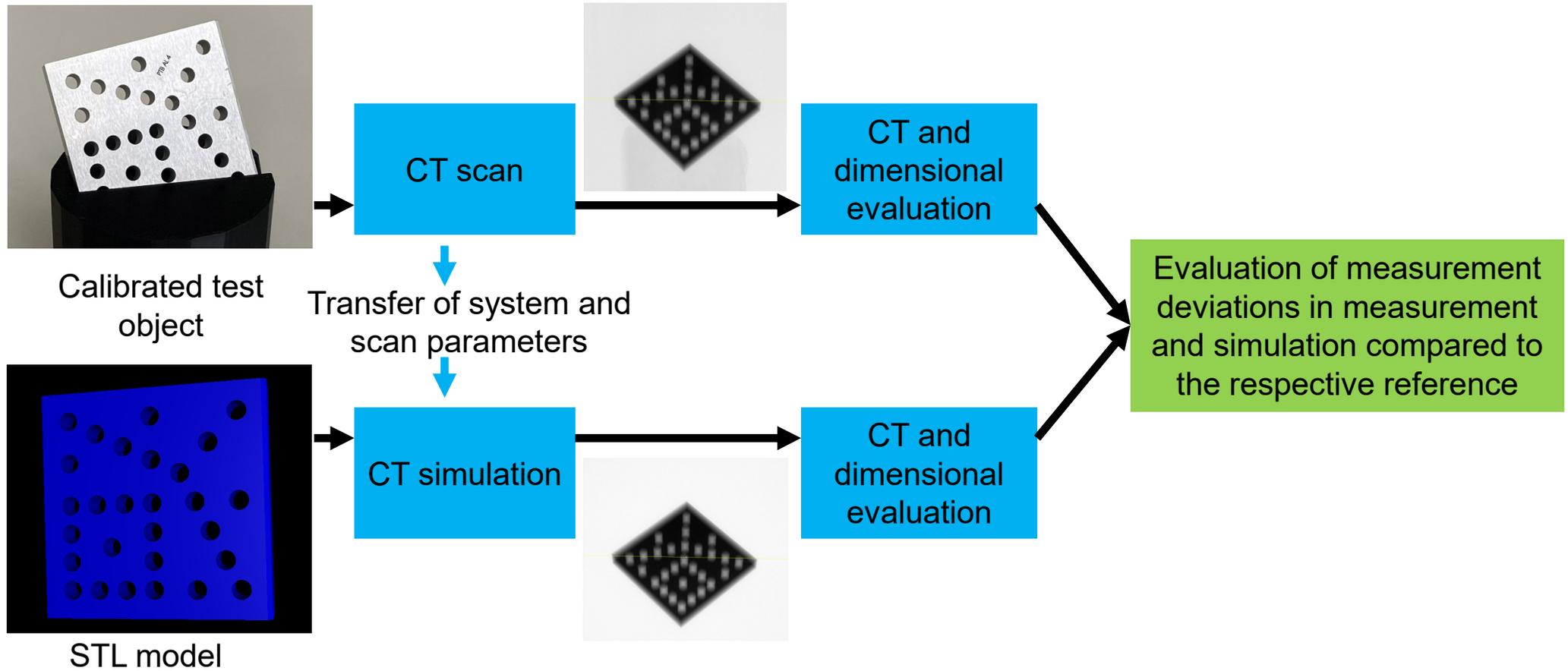
Test to validate the digital model (Step-T)



Requirements for and testing of the digital model

- Definition of minimum requirements for the digital model (derived from the defined JSON interface from CTSimU1)
- Test concept based on modified metrological compatibility of repeated measurements on calibrated material standards
 - Comparison of the results of the digital model with real measurement results in terms of metrological compatibility
 - Identification of suitable deviation limits
 - Documentation of the defined minimum requirements
 - Examination of the test concept with regard to borderline cases/failures/external influences
 - Definition of the test procedure

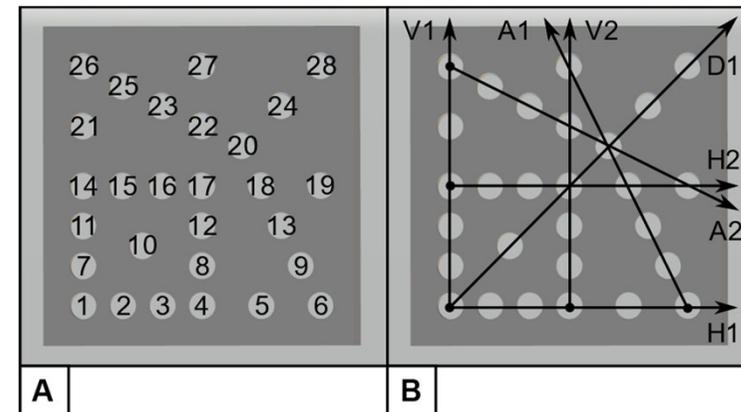
	Effects	Model
X-ray source	Spot size	✓
	Intensity distribution	✓/✗
	Spectrum	✓
	Spot drift	✗
Detector	Detector geometry (pixel size, number)	✓
	Scintillator thickness	✓
	Scintillator material	✓
	Noise	✓
	Back scattering	✗
	Unsharpness	✓
System geometry	Modelling of the measurement trajectory (calibration, manipulator translations)	✓
	Dynamic deviations of the rotary table	✓/✗
	Positioning accuracy of manipulator (translation)	✗
Test object	Positioning of the test object	✓
	Manufacturing deviations of the actual test object	✗
	Scattered radiation	✓



Example: Repeated measurements of calibrated aluminium hole plate (10 repeated measurements)

Scan parameters:

Acceleration voltage	150 kV
Tube current	180 μ A
Exposure time	2 s
Number of projections	2050
Magnification	4.9
Voxel size	40.7 μ m
Pre-filter	0.5 mm Copper



Source: Felix Binder *et al* 2022 *Meas. Sci. Technol.* **33** 104002

Size: 48 x 48 x 8 mm³

Quantities:

- 28 Hole diameters
- 35 Centre-to-centre distances

X-ray source

- **Calculated polychromatic spectrum** (Target type, Tube geometry, Source filter, Tube voltage)
- **Gaussian spot** (power)

Scan geometry and workpiece



- **Calibrated trajectory**
- **Digital workpiece model with nominal geometry and aluminium alloy according to data sheet**
- **Orientation of the workpiece in the measuring volume derived from actual measurement**
- **Scattered radiation**

Detector and image

- **Detector characteristic curve** (scintillator material and thickness)
- **Linear energy to grey value characteristic**
- **Noise** (SNR at maximum grey value)
- **Blurring** (iSrb and long range unsharpness)

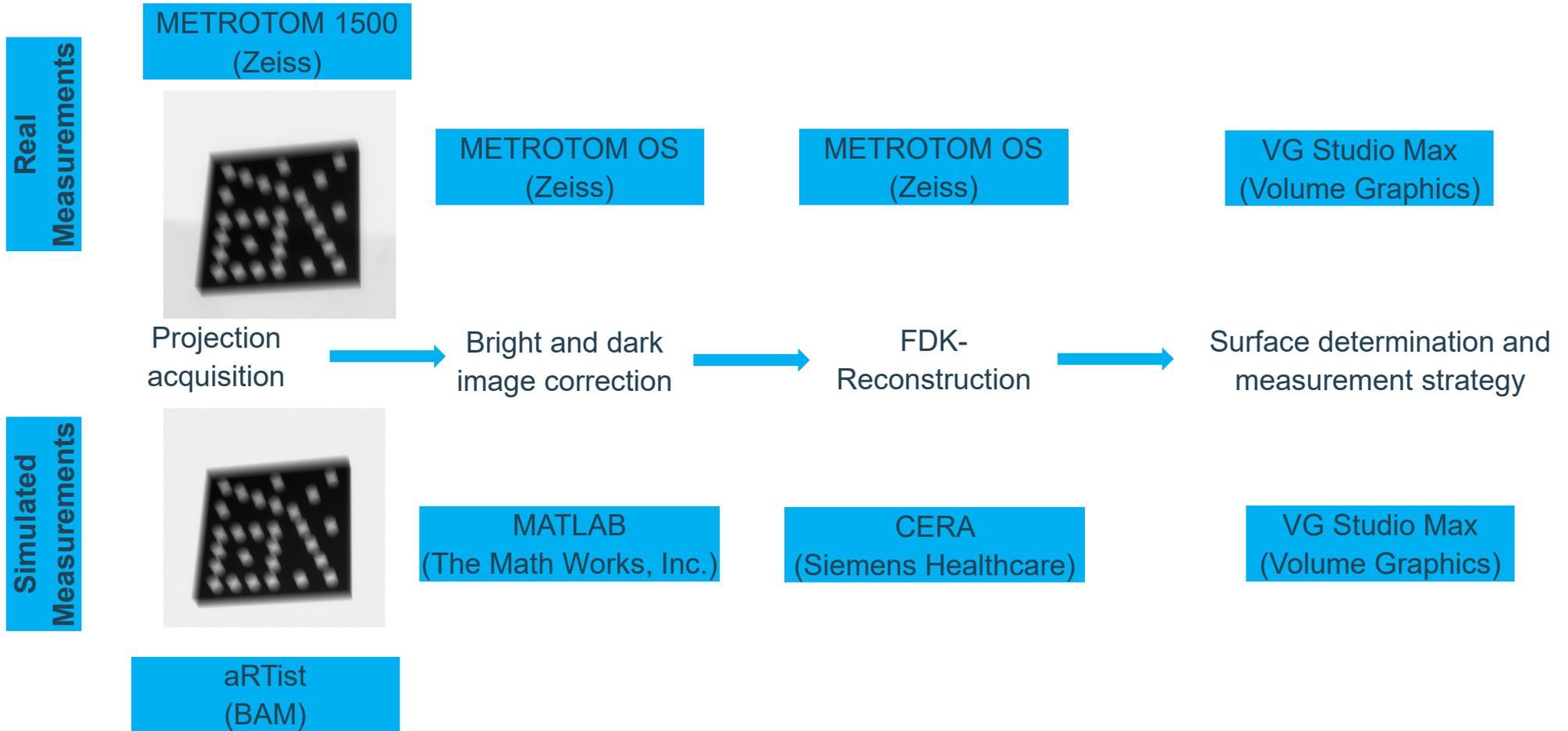
All input parameters were assumed to be static nominal values

→ Variance in measurement values results only from noise and scattered radiation

CTSimU2

Evaluation - Workflow

Repeated measurements of a calibrated aluminium hole plate





Actual measurement is subject to external influences (e.g. calibration, temperature) → Uncertainty analysis

Measurement:

Measurement uncertainty based on VDI 2630 Part 2.1 (adapted for repeated measurements)

$$U_{\text{meas}}(\bar{x}_{\text{meas}}) = k \cdot \sqrt{u_{\text{cal}}^2 + \left(\frac{u_{\text{p,meas}}}{\sqrt{n}}\right)^2 + u_{\text{b}}^2}$$

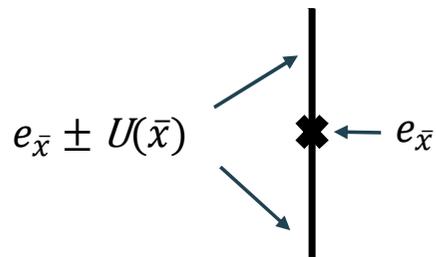
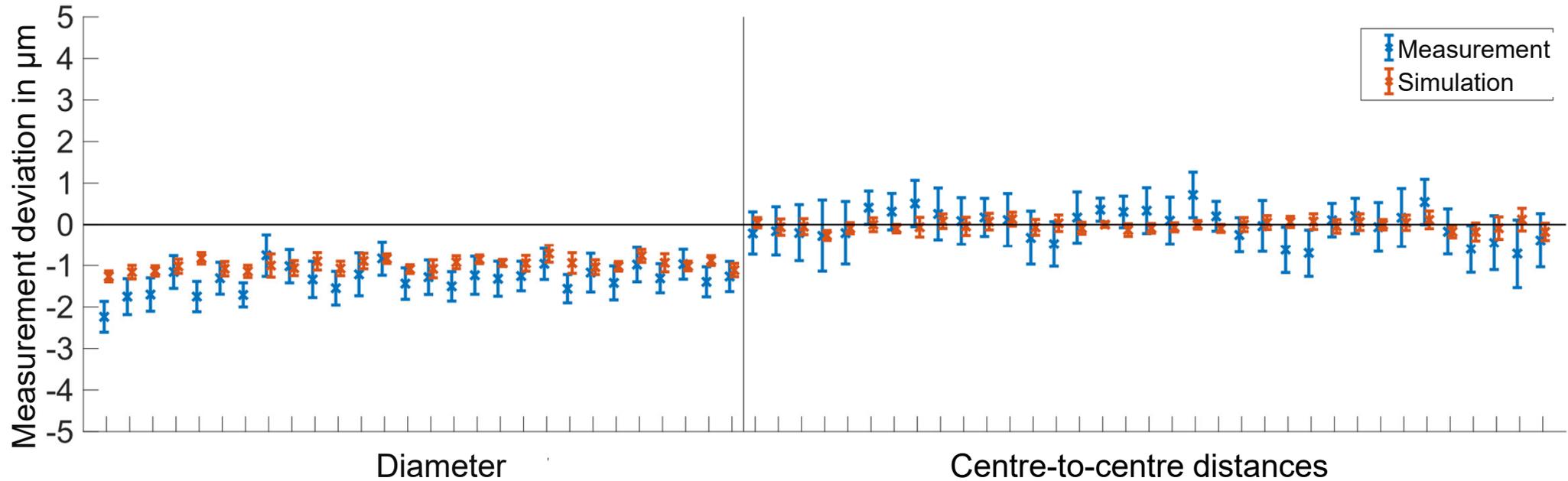
For a detailed description of the procedure shown here, see also: M. Braun *et. al.*, „Simulation of a real dimensional CT measurement study using a calibrated aluminum specimen“, doi: 10.58286/31414

- $U(\bar{x})$: expanded measurement uncertainty for the mean value \bar{x}
- u_{p} : standard deviation of repeated CT measurements
- u_{cal} : standard calibration uncertainty
- u_{b} : uncertainty of the correction of the systematic error (here: only temperature!)
- n : number of repeated measurement
- k : coverage factor

Simulation:

Uncertainty due to noise and scattered radiation

$$U_{\text{sim}}(\bar{x}_{\text{sim}}) = k \cdot \frac{u_{\text{p,sim}}}{\sqrt{n}}$$



$$e_{\bar{x}} = \bar{x} - x_{\text{ref}}$$

$$U_{\text{meas}}(\bar{x}_{\text{meas}}) = k \cdot \sqrt{u_{\text{cal}}^2 + \left(\frac{u_{p,\text{meas}}}{\sqrt{n}}\right)^2 + u_{\text{b}}^2}$$

$$U_{\text{sim}}(\bar{x}_{\text{sim}}) = k \cdot \frac{u_{p,\text{sim}}}{\sqrt{n}}$$

Sufficient agreement between measurement and simulation?

Test criterion: Adapted approach for the E_n value according to (DIN EN ISO/IEC 17043:2023)

$$E_{n,DM} = \frac{(\bar{x}_{sim} - x_{ref,sim}) - (\bar{x}_{meas} - x_{ref,meas})}{\sqrt{U_{sim}^2(\bar{x}_{sim}) + U_{meas}^2(\bar{x}_{meas})}}$$

$E_{n,DM}$: normalized error of the digital model
 \bar{x} : mean measured value
 x_{ref} : reference value

$$|E_{n,DM}| \leq 1$$

→ The difference between the simulated and measured mean values of the systematic measurement deviation is smaller than the associated uncertainty of this difference.

$$|E_{n,DM}| \leq \sqrt{n}$$

→ A digital model does not require the implementation of distributions of relevant influencing factors. Depending on the application, it may be sufficient for the digital model to meet a weaker requirement. (no direct mathematical interpretation of the limit value)

Adaptation of the E_n value demands boundary conditions in order to maintain the significance of the parameter

Boundary conditions

1. The calibration uncertainty must be sufficiently smaller than the standard deviation of the CT repeated measurements.

$$\text{a) } q_{\text{cal}} = \frac{u_{\text{cal}}}{u_{\text{p,meas}}} \leq q_{\text{l,cal}}$$

2. The standard deviation of the simulated measurement must not exceed a certain level relative to the standard deviation of the actual CT measurement.

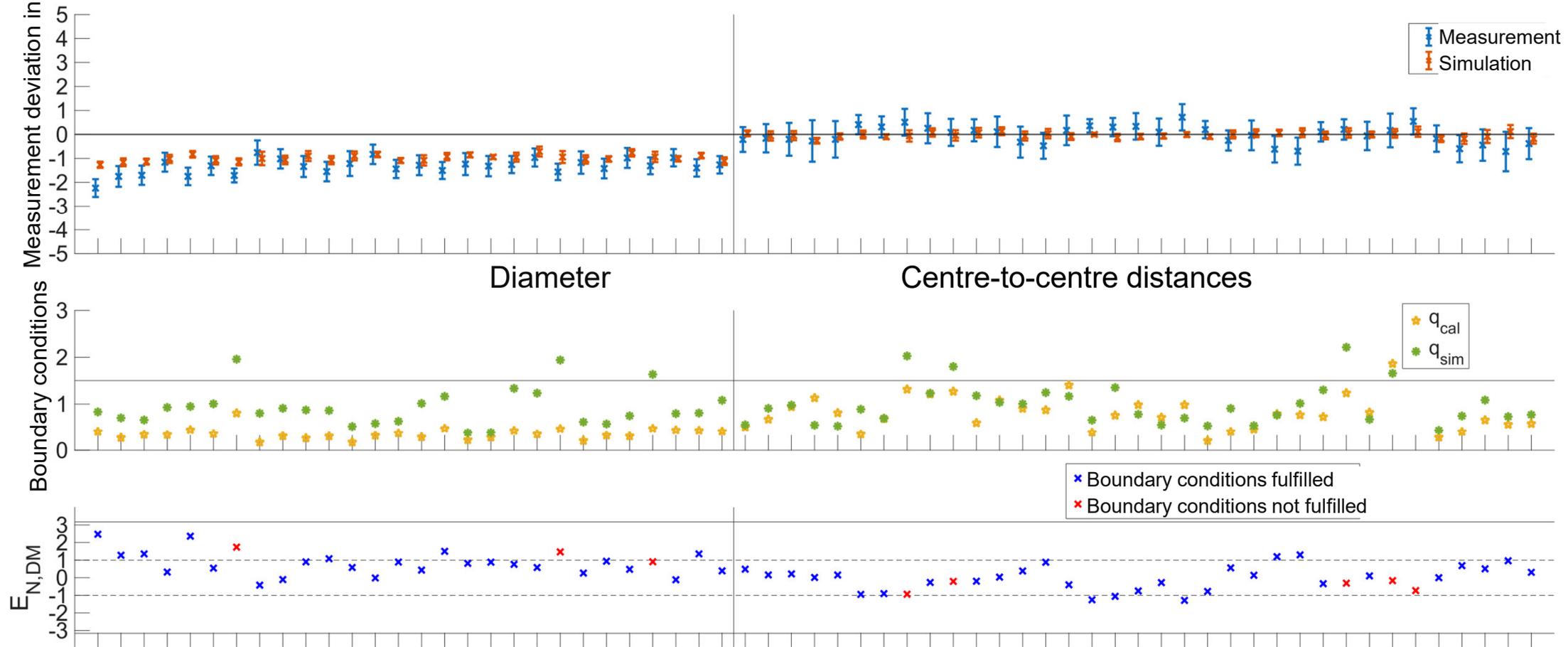
$$\text{b) } q_{\text{sim}} = \frac{u_{\text{p,sim}}}{u_{\text{p,meas}}} \leq q_{\text{l,sim}}$$

u_{p} : Standard deviation of repeated CT measurements

u_{cal} : Standard calibration uncertainty

$q_{\text{l,cal}}$: Maximum ratio

For $q_{\text{l,cal}}$ and $q_{\text{l,sim}}$, for example, 1.5 can be selected in each case.



Comprehensive literature review and systematisation of methods for obtaining parameters



Review article about the methods for characterising a real CT system is currently being drafted

Parameter acquisition from real CT systems, modelling and parameter evaluation as well as parameter conversion for simulation software



Improvement and extension of the simulation file interface (JSON)

Development of the test to verify whether the digital model accurately reflects the dimensional measurements



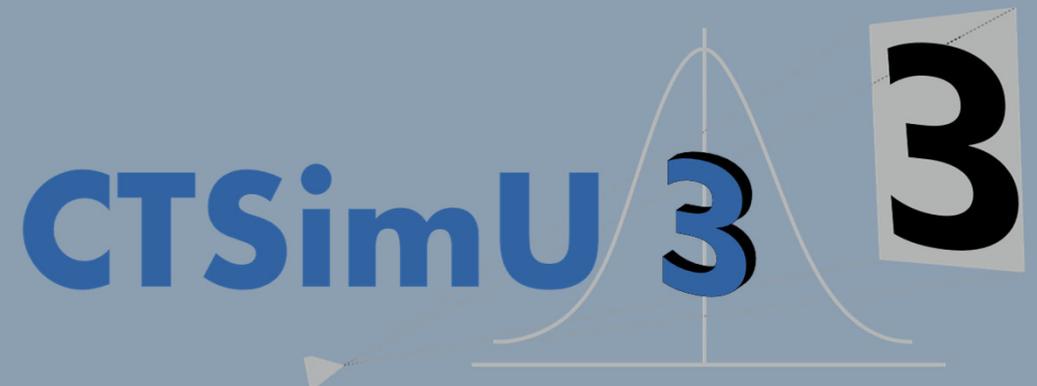
Further improvement and extension of the image processing toolbox and application of the test with various calibrated material standards (<https://bamresearch.github.io/ctsimu-toolbox/>)

Result:

Draft of a standard for VDI/VDE 2630 series

Submission to VDI/VDE-GMA Technical Committee 4.33 'Computed tomography in dimensional measurement' for finalisation

CTSimU3



Evaluation of the uncertainty of X-ray computed tomography measurements of geometric features through simulation

Consortium: 4 research partners, 7 industrial partners, 5 associated partners



Evaluation of MU: Identification and prioritisation of the key influences on MU in CT, evaluation of influence factor distributions (how and which influence factors vary on which time scales), toolbox for Monte Carlo simulation and evaluation (discrete distributions, estimated values of measured quantities and coverage intervals), identification of simulation termination criteria, verification.

Verification that the evaluated MU is stable and reliable according to the state of the art and that it accurately reflects the real uncertainty.

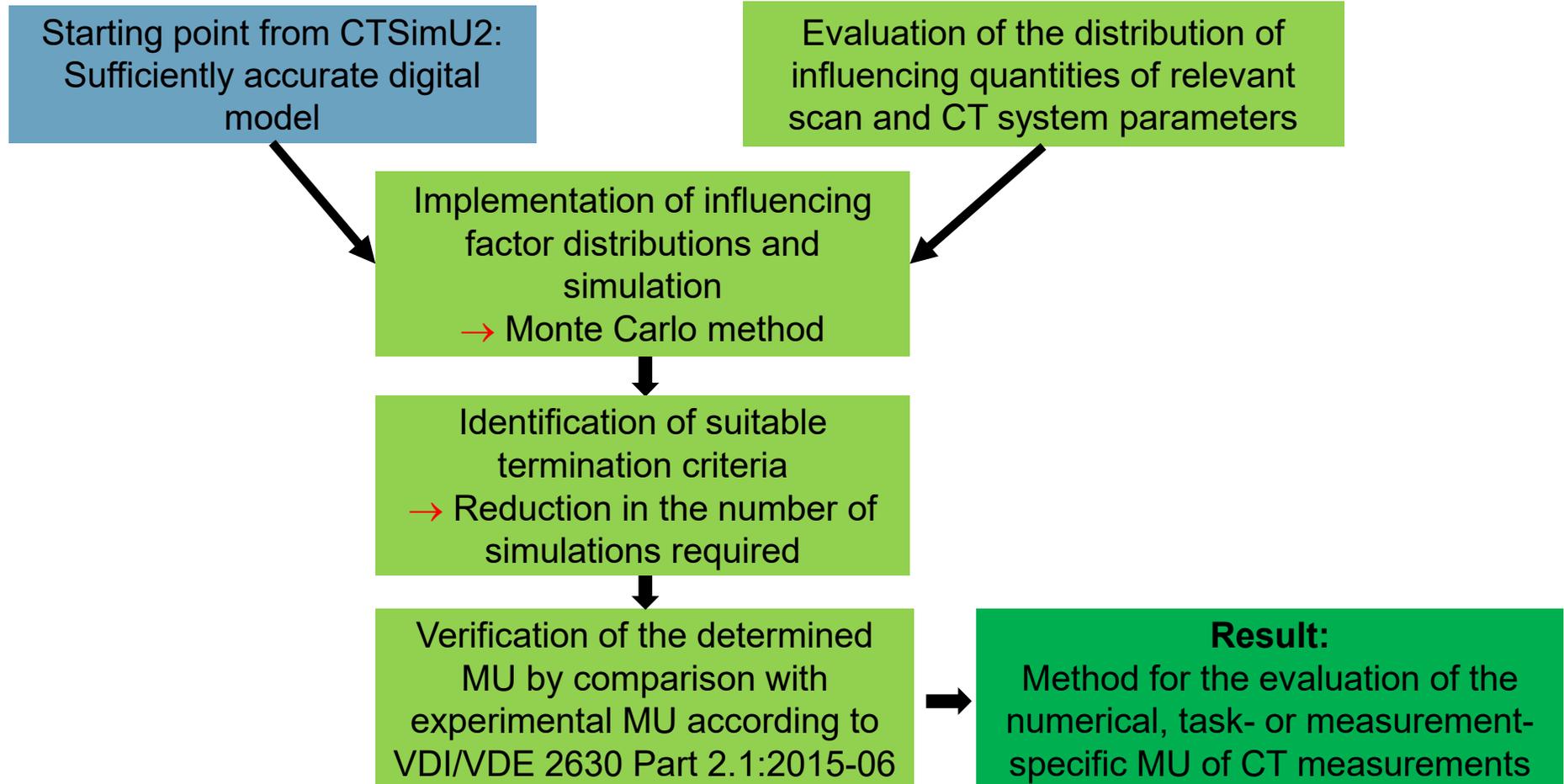
Draft of a standard for VDI/VDE 2630 series 'Computed tomography in dimensional measurement'



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CTSimU3

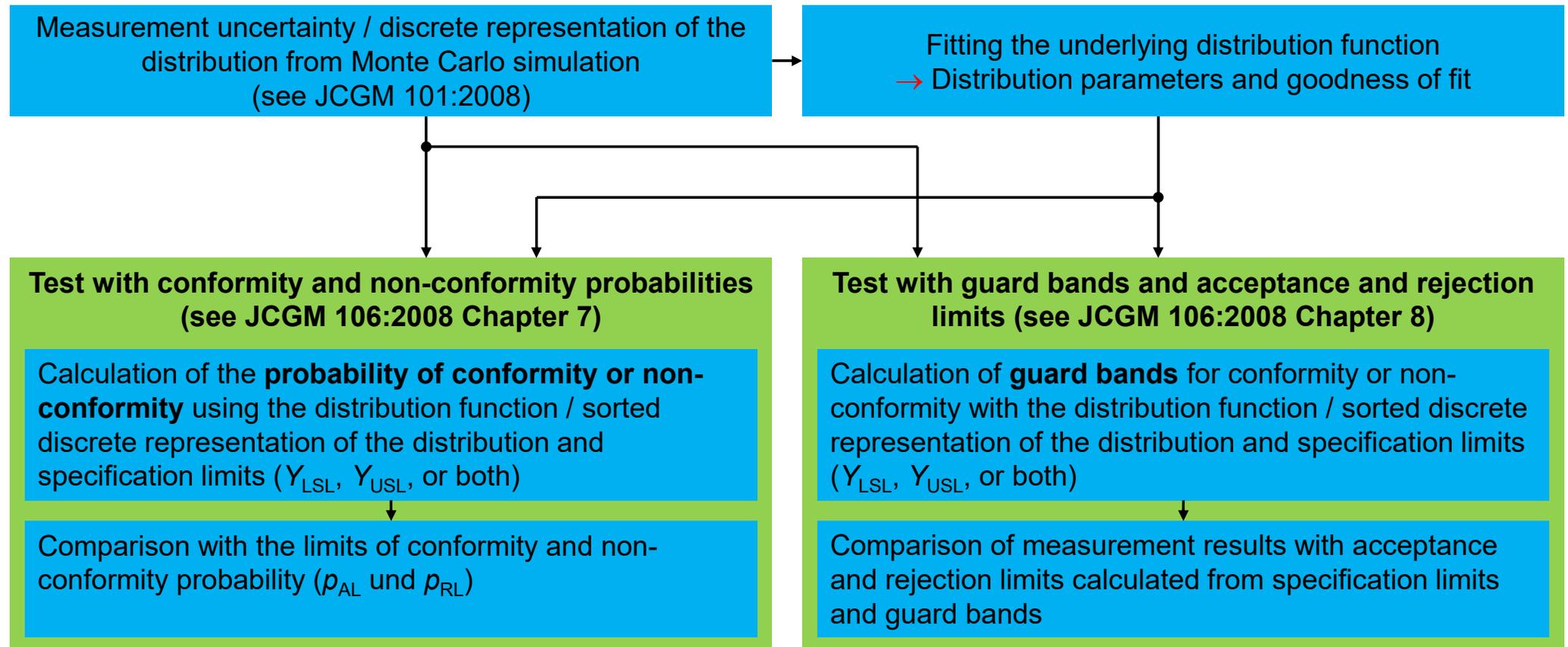
Determination of the uncertainty of X-ray computed tomography measurements of geometric features by simulation



Application of Monte Carlo simulation results for conformity or non-conformity assessment

Application of Monte Carlo simulation result

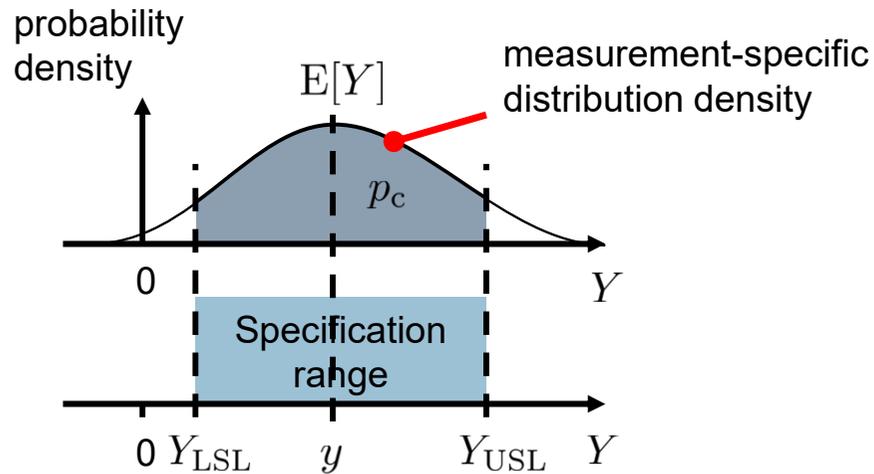
Possible overall process for conformity and non-conformity assessment



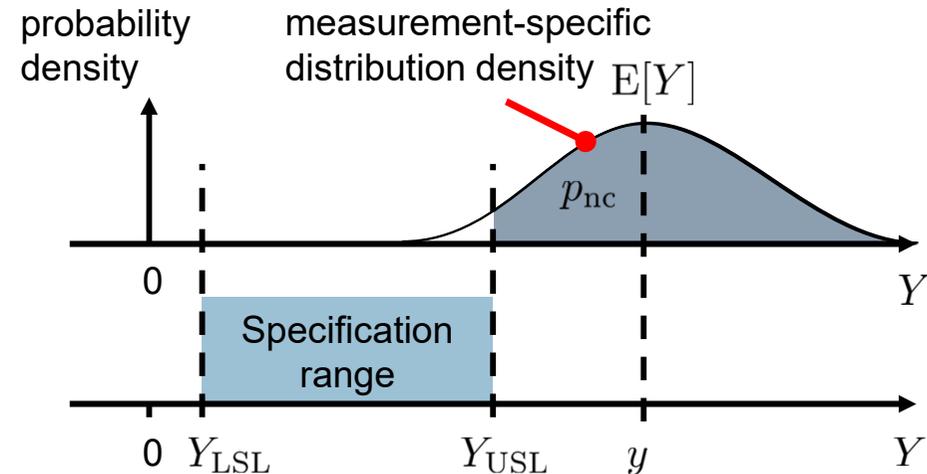
Conformity and non-conformity assessment

Test with conformity and non-conformity probabilities (see JCGM 10:2008 Chapter 7)

Conformity assessment



Non-conformity assessment



Y measurand and y measured value

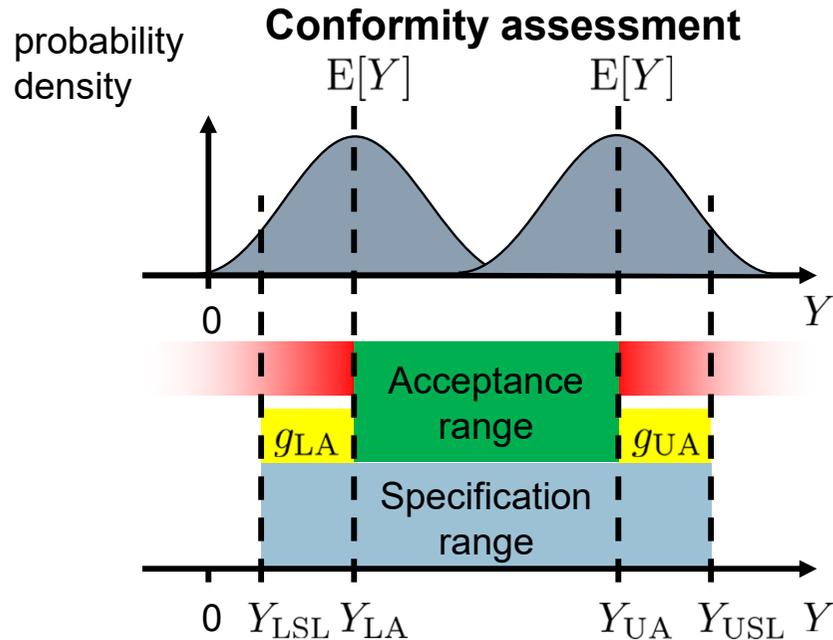
Y_{LSL} and Y_{USL} lower and upper specification limits

p_c and p_{nc} Probability of conformity and probability of non-conformity

p_{AL} and p_{RL} Limits of conformity probability and non-conformity probability

Conformity and non-conformity assessment

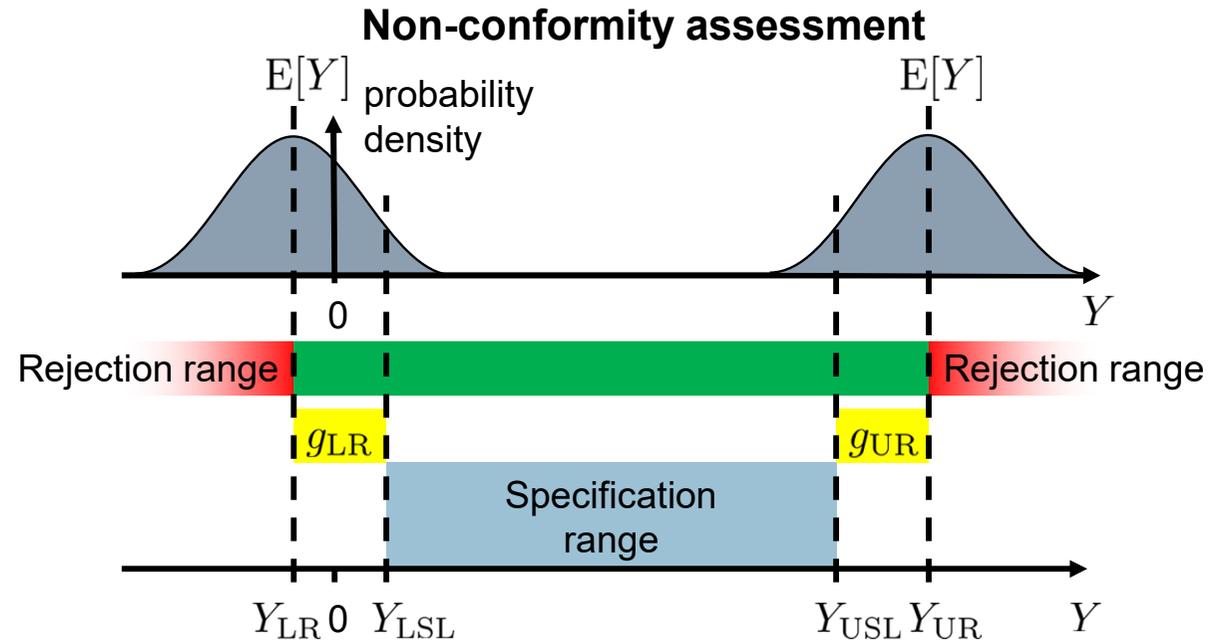
Test with guard bands and acceptance and rejection limits (see JCGM 106:2008 Chapter 8)



Y measurand

g_{LA} and g_{UA} guard bands

Y_{LA} and Y_{UA} smallest and largest measured value for which conformity can be confirmed



Y_{LSL} and Y_{USL} lower and upper specification limits

g_{LR} and g_{UR} guard bands

Y_{LR} and Y_{UR} smallest and largest measured value for which non-conformity can be confirmed

Impact of the project series on standardization

The work in the project series directly or indirectly influences standardisation work in the following committees:

- VDI/VDE-GMA Technical Committee 4.33 “Computed tomography in dimensional measurement”
- VDI/VDE-GMA Technical Committee 4.31 / DIN NA 152-03-02-12 GUA “Coordinate measuring technology”
- ISO/TC 213 Dimensional and geometrical product specifications and verification
 - WG 10 Coordinate measuring machines (German mirror committee: DIN NA 152-03-02-12 GUA “Coordinate measuring technology”)
- VDI/VDE-GMA Technical Committee 1.12 “Measurement uncertainty and test process suitability”
- German Society for Non-Destructive Testing (Deutsche Gesellschaft für Zerstörungsfreie Prüfung, DGZfP) Subcommittee (UA) CT
- ISO/TC 213 Dimensional and geometrical product specifications and verification
 - WG 4 Uncertainty of measurement and decision rules (German mirror committee: DIN NA 152-03-02 AA CEN/ISO “Geometric product specification and verification”)

Summary

Summary

- Motivation for the CTSimU project series and fundamentals
- Motivation, objectives, and results for the projects CTSimU1 and CTSimU2
- Motivation, objectives, and approach for the started project CTSimU3
- Application of Monte Carlo simulation results for conformity or non-conformity assessment
- Impact of the project series on standardisation

Outlook

- Upon completion of the CTSimU3 project, the results of the project series will hopefully lead to better acceptance of CT for dimensional measurements and to optimisation of CT measurements.

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Thank you
for your attention!

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